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The following reference list only includes textbooks and monographs, thus disregarding papers in scientific journals, congress proceedings, research and technical reports, and so on. Our choice aims at limiting the number of citations, in line with the teaching orientation of this work. For more detailed presentations of the various topics, the reader can also refer to the lists of references provided by the several monographs, all quoted below, we have cited in the final section of each chapter.


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