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Sean A. Fulop

# Speech Spectrum Analysis

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*For Billy, who helped me write this.*

# Preface

The analysis and measurement of the spectrum of a speech signal is one of the most important areas of sound signal processing for a number of fields, yet it is not an area to which a book has been specifically devoted. The accurate determination of the speech spectrum is commonly pursued in diverse areas including speech processing, recognition, and acoustic phonetics. With this book I hope to make the subject of spectrum analysis understandable to a wide audience, which I imagine could include those with a solid background in general signal processing (but not necessarily in speech), and also speech scientists and students with some acoustic phonetics experience who have limited knowledge of signal processing. In keeping with these goals, this is not a book that replaces or attempts to cover the material found in a general signal processing textbook. Some essential signal processing concepts are presented in [Chap. 2](#), but even there the concepts are presented in a generally understandable fashion as far as is possible. Throughout the book, the focus will be on applications to speech analysis and the measurement of important descriptive speech parameters. No attention is paid to parametrizing speech purely for coding or decorrelation for further processing. Mathematical theory will be provided for completeness, but many of these developments are set off in boxes for the benefit of those readers with sufficient background. Other readers may proceed through the main text, where the key results and applications will be presented in plain language as far as possible, and illustrated with software routines and practical “show-and-tell” discussions of the results.

At some points, the book refers to and uses the implementations in the Praat speech analysis software package, which has the advantages that it is used by many scientists around the world, and it is free and open source software, obtainable on the internet from the Praat homepage. At other points, special software routines have been developed and made available to complement the book, and these are provided in the Matlab programming language. If the reader has the basic Matlab package, he/she will be able to immediately implement most of the programs in that platform—only [Chap. 7](#) requires the extra Signal Processing toolbox. A few other freely available toolboxes are also needed, and all the Matlab code is made available for download at the Springer website for additional materials.

And finally, as was written by Lord Kelvin and Professor Tait in their *Treatise on Natural Philosophy* (1912), “I confidently hope that few erratums of serious note will now be found in the work.”

Fresno, October 2010

Sean Fulop

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